

Cambridge O Level

ADDITIONAL MATHEMATICS**4037/21**

Paper 2

May/June 2025

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2025 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

This document consists of **12** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

Annotations guidance for centres

Examiners use a system of annotations as a shorthand for communicating their marking decisions to one another. Examiners are trained during the standardisation process on how and when to use annotations. The purpose of annotations is to inform the standardisation and monitoring processes and guide the supervising examiners when they are checking the work of examiners within their team. The meaning of annotations and how they are used is specific to each component and is understood by all examiners who mark the component.

We publish annotations in our mark schemes to help centres understand the annotations they may see on copies of scripts. Note that there may not be a direct correlation between the number of annotations on a script and the mark awarded. Similarly, the use of an annotation may not be an indication of the quality of the response.

The annotations listed below were available to examiners marking this component in this series.

Annotations

Annotation	Meaning
	More information required
	Accuracy mark awarded zero
	Accuracy mark awarded one
	Accuracy mark awarded two
	Accuracy mark awarded three
	Independent mark awarded zero
	Independent mark awarded one
	Independent mark awarded two
	Independent mark awarded three
	Benefit of the doubt
	Communication mark
	Incorrect
	Follow through
Highlighter	Highlight a key point in the working
	Ignore subsequent work
	Method mark awarded zero
	Method mark awarded one
	Method mark awarded two
	Method mark awarded three

Annotation	Meaning
MR	Misread
O	Omission
Off-page comment	Allows comments to be entered at the bottom of the RM marking window and then displayed when the associated question item is navigated to.
On-page comment	Allows comments to be entered in speech bubbles on the candidate response.
Pre	Premature rounding/approximation
SC	Special case
SEEN	Indicates that work/page has been seen
TE	Transcription error
	Correct
XP	Correct answer from incorrect working

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

M Method marks, awarded for a valid method applied to the problem.

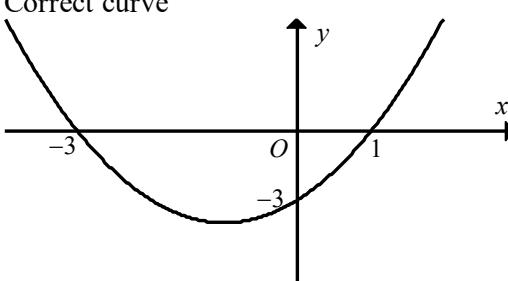
A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.

B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘dep’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfww	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Partial Marks
1(a)	$(x+1)^2 - 4$ oe $(-1, -4)$	B3	B2 $y = (x+1)^2 - 4$ oe or B1 $y = (x+1)^2 + k$, where k is a constant
1(b)	Correct curve 	B2	B1 for correct shape in 4 quadrants with minimum in the 3rd quadrant B1 for an attempt at a quadratic graph with intercepts marked at -3 on the y-axis and -3 and 1 on the x-axis
2	$(3k-2)^2 - 4(2)(k) [*0]$	M1	Uses $b^2 - 4ac$ * could be any inequality sign or =
	$9k^2 - 20k + 4 [*0]$	A1	Correctly simplifies to 3-term quadratic
	$(9k-2)(k-2)$	M1	FT Factorises or solves <i>their</i> 3-term quadratic
	Critical values $\frac{2}{9}, 2$	A1	
	$k < \frac{2}{9}$ $k > 2$	A1	Mark final answer
3(a)	103 680	2	M1 for $k \times 5! \times 4! \times 3!$ where $k = 1, 2, 3, 6$
3(b)	270	3	M2 for ${}^5C_1 \times {}^4C_2 \times {}^3C_1 + {}^5C_1 \times {}^4C_1 \times {}^3C_2 +$ ${}^5C_2 \times {}^4C_1 \times {}^3C_1$ oe OR M1 for at least one correct product If 0 scored then SC1 for a <u>final</u> answer of 540 or 264

Question	Answer	Marks	Partial Marks
4	$m_{AB} = \frac{-9-3}{6-4}$ oe isw or $-\frac{6}{5}$	M1	
	$[m_{\perp}] = \frac{5}{6}$ or $\frac{-1}{\text{their } m_{AB}}$	M1	FT <i>their</i> m_{AB} providing that difference in y attempted difference in x
	[Midpoint] $\left(\frac{-4+6}{2}, \frac{3-9}{2}\right)$ oe isw or $(1, -3)$	M1	
	Finds equation of perpendicular bisector: $y - \text{their } (-3) = -\frac{1}{\text{their } \left(-\frac{6}{5}\right)}(x - \text{their } 1)$ oe	M1	FT <i>their</i> perpendicular gradient providing gradient is $-\frac{1}{\text{their } m_{AB}}$ and using <i>their</i> midpoint <i>Their</i> midpoint must not be any of A, B, C or D
	$11x - 75 = \frac{5}{6}x - \frac{23}{6}$	M1	Eliminates one variable dep on previous M mark $11x - 75 = \text{their perp bisector equation}$
	$E(7, 2)$	A1	
5	[Area $CDE =] 40$	A1	Dependent on all previous marks
	$\frac{dy}{dx} = 2x \tan \frac{x}{2} + \frac{x^2}{2} \sec^2 \frac{x}{2}$ oe	2	B1 for $\frac{d}{dx} \left(\tan \frac{x}{2} \right) = \frac{1}{2} \sec^2 \frac{x}{2}$ soi or M1 FT for a product rule of correct structure with <i>their</i> $\frac{d}{dx} \left(\tan \frac{x}{2} \right)$
	$\frac{\delta y}{h} = \text{their} \frac{dy}{dx} \Big _{x=\frac{\pi}{3}}$ or $\text{their} \frac{dy}{dx} \Big _{x=\frac{\pi}{3}} \times h$	M1	Correct small changes relationship
6(a)	1.94h	A1	Dependent on B2
	$(3x + 2)^{10}$ oe	M2	M1 for $(3x + 2)^2$ soi
	$1024 + 15360x + 103680x^2$	A2	A1 for any two terms correct or $2^{10} + 10(2^9)(3x) + 45(2^8)(3x)^2$ or for 3 correct terms seen but not summed e.g. a list After M2 A0 , allow SC1 for an answer of $59049x^{10} + 393660x^9 + 1180980x^8$

Question	Answer	Marks	Partial Marks
6(b)	51 963 120	2	M1 for $^{12}C_4 \left(\frac{6}{x^2}\right)^8 \left(\frac{x^4}{2}\right)^4$ soi
7(a)	Correct pair of graphs with both asymptotes and both intercepts correctly shown	4	<p>B1 for correct shape for f; must have positive y-intercept and appear to tend to an asymptote in the 1st quadrant</p> <p>B1 for $(0, 5)$ indicated; must have attempted correct shape for f</p> <p>B1 for asymptote at $y = 3$; must have attempted correct shape for f</p> <p>B1 for a correct reflection of <i>their</i> f in the line $y = x$</p> <p>$y = x$ does not have to be drawn</p> <p>Maximum of B3 if not fully correct</p>
7(b)	$e^y = \frac{3}{2-x} - 2$ oe OR $e^x = \frac{3}{2-y} - 2$ oe and variables swapped at some point	M1	Rearranges to $e^y = \dots$ e.g. $e^y = \frac{2x-1}{2-x}$ or $e^y = \frac{1-2x}{x-2}$ or $e^y = \frac{-3}{x-2} - 2$
	$\ln\left(\frac{3}{2-x} - 2\right)$ oe, isw	A1	
	$1 \leq x < 2$	B2	B1 $x \geq 1$ oe OR $x < 2$ oe OR $1 < x \leq 2$
8(a)	$\cos x = 0$ or $\tan x = \frac{3}{2}$ oe	M1	
	$[x =] \frac{\pi}{2}$ or $1.57[07\dots]$ 0.983 or $0.9827[93\dots]$	A2	and no extra solutions in range A1 for either ignoring extras
8(b)	$\frac{2}{\sin(2\theta+1)} - 12\sin(2\theta+1) = 5$ or $2\cosec(2\theta+1) - \frac{12}{\cosec(2\theta+1)} = 5$	M1	<ul style="list-style-type: none"> Writes in terms of $\cosec(2\theta+1)$ or $\sin(2\theta+1)$ only.

Question	Answer	Marks	Partial Marks
	$12\sin^2(2\theta+1) + 5\sin(2\theta+1) - 2 [=0]$ or $2\csc^2(2\theta+1) - 5\csc(2\theta+1) - 12 [=0]$ oe	A1	
	$4\sin(2\theta+1) - 1)(3\sin(2\theta+1) + 2) [=0]$ or $(2\csc(2\theta+1) + 3)(\csc(2\theta+1) - 4) [=0]$	M1	Factorises or solves <i>their</i> 3-term quadratic in $\sin(2\theta+1)$ or $\csc(2\theta+1)$ dep on previous M1
	$2\theta+1 = 0.253$ or $0.2526[80\dots]$ OR $2\theta+1 = -0.73[0]$ or $-0.7297[27\dots]$ OR $2\theta+1 = \sin^{-1}\left(\text{their } \frac{1}{4}\right)$ OR $2\theta+1 = \sin^{-1}\left(\text{their } -\frac{2}{3}\right)$	M1	dep on previous M1 FT providing $-1 \leq \text{their } \frac{1}{4} \leq 1$ and/or $-1 \leq \text{their } -\frac{2}{3} \leq 1$
	-0.374 or $-0.3736[59\dots]$ 0.944 or $0.9444[56\dots]$ -0.865 or $-0.8648[63\dots]$ 1.44 or $1.435[66\dots]$	A2	and no extra solutions in range A1 for two correct solutions ignoring extras in range
9(a)	135π isw or 424 or 424.1 to 424.2	2	M1 for $\frac{1}{2} \times 15^2 \times \frac{6\pi}{5}$ oe
9(b)	18π or 56.5 to 56.6	2	M1 for $15 \times \frac{6\pi}{5}$ oe
9(c)	radius = 9, height = 12	2	B1 for radius = 9 OR M1 for a correct Pythagoras' statement e.g. <i>their</i> $r^2 + \text{height}^2 = 15^2$
9(d)(i)	$r = \frac{3}{4}h$ oe	B1	

Question	Answer	Marks	Partial Marks
9(d)(ii)	$V = \frac{1}{3} \pi \left(\frac{3}{4}h\right)^2 \times h$ oe	B1	FT <i>their</i> $r = kh$ where k is a positive constant e.g. $V = \frac{1}{3} \pi (\text{their } kh)^2 \times h$
	$\frac{dV}{dh} = \frac{9\pi h^2}{16}$ oe	B1	FT <i>their</i> k where k is a positive constant e.g. $\frac{dV}{dh} = (\text{their } k)^2 \pi \times h^2$
	Relevant, correct chain rule including $\frac{dh}{dt}$ soi $\frac{dh}{dt} = \frac{dV}{dt} \times \frac{dh}{dV}$ oe	B1	e.g. $\frac{dh}{dt} = \frac{dV}{dt} \div \frac{dV}{dh}$
	$27 \times \frac{16}{9\pi \times 16}$ oe	M1	
	0.955 or 0.9549[29...]	A1	
10(a)(i)	$[v =] \frac{t^3}{3} - 2t$ (+c)	M1	Or $\left[\frac{t^3}{3} - 2t \right]_{[3]}^{[4]}$
	$[v =] \frac{t^3}{3} - 2t - \frac{10}{3}$	A1	Or substituting in limits $\left(\frac{4^3}{3} - 2 \times 4 \right) - \left(\frac{3^3}{3} - 2 \times 3 \right) - \frac{1}{3}$
	$v = 10$	A1	
10(a)(ii)	2 correct terms in $[s =] \frac{t^4}{12} - t^2 - \frac{10}{3}t$ (+d)	M1	FT an expression in form $at^3 + bt$ Or 2 correct terms in $\left[\frac{t^4}{12} - t^2 - \frac{10}{3}t \right]_{[3]}^{[4]} 1$
	$s = \frac{t^4}{12} - t^2 - \frac{10}{3}t + 12$	A1	A1 substituting in limits $\left(\frac{4^4}{12} - 4^2 - \frac{10}{3} \times 4 \right) - \left(\frac{3^4}{12} - 3^2 - \frac{10}{3} \times 3 \right) - \frac{1}{4}$
	$s = 4$	A1	

Question	Answer	Marks	Partial Marks
10(b)	$[v =] 19t + \frac{5}{2}e^{8-2t} (+c) \text{ oe}$	M1	
	$[v =] 19t + \frac{5}{2}e^{8-2t} - \frac{137}{2} \text{ oe}$	A1	FT (their 10) – 78.5
	$[s =] \frac{19t^2}{2} - \frac{5}{4}e^{8-2t} - \frac{137}{2}t (+d) \text{ oe}$	M1	dep on previous M1 FT their $-\frac{137}{2}$ provided not 0 or algebraic
	$[s =] \frac{19t^2}{2} - \frac{5}{4}e^{8-2t} - \frac{137}{2}t + \frac{509}{4} \text{ oe, cao}$	A1	
	$s = 392 \text{ or } 392.2[49\dots]$	A1	
11(a)	$ar + ar^2 = 168 \text{ or } ar^3 + ar^4 = 94.5 \text{ oe soi}$	B1	
	$\frac{ar^3(1+r)}{ar(1+r)} = \frac{94.5}{168} \text{ oe}$	M1	Correct equation where a can be directly eliminated
	$168r^2 = 94.5 \text{ oe}$	M1	
	$r = \frac{3}{4} \text{ only nfww}$	A1	
	$\frac{3}{4}a + \frac{9}{16}a = 168 \text{ oe}$	M1	FT their r
	$a = 128$	A1	
	$u_6 = \frac{243}{8} \text{ only oe, isw}$	B1	
11(b)	512	B1	